

# 01 Linear Inequalities

Wednesday, November 28, 2018

8:09 AM



## 01 Linear Inequalities

$$\begin{aligned}
 9x - 7i &> 3(3x - 7u) \\
 9x - 7i &> 9x - 21u \\
 -7i &> 9x - 9x - 21u \\
 -7i &> -21u \\
 i &< -21u \\
 i &< 3u
 \end{aligned}$$

A linear inequality in two variables may come in two forms:

$$\begin{aligned}
 \frac{y \geq 3x + 2}{4x + 2y \geq 10} \quad m = 3 \quad y\text{-int} = 2 \\
 y = mx + b
 \end{aligned}$$

An inequality in 2 variables defines an infinite area in the cartesian plane.

Any point (x, y) that satisfies the inequality is a solution.

Eg: Which points are solutions?

$$\begin{aligned}
 3x - 2y &\geq -16 \\
 3(-3) - 2(4) &\geq -16 \\
 -9 - 8 &\geq -16 \\
 -17 &\geq -16 \quad \times \\
 3(0) - 2(2) &\geq -16 \\
 -4 &\geq -16 \quad \checkmark \\
 3(-5) - 2(3) &\geq -16 \\
 -15 - 6 &\geq -16 \\
 -21 &\geq -16 \quad \times
 \end{aligned}$$

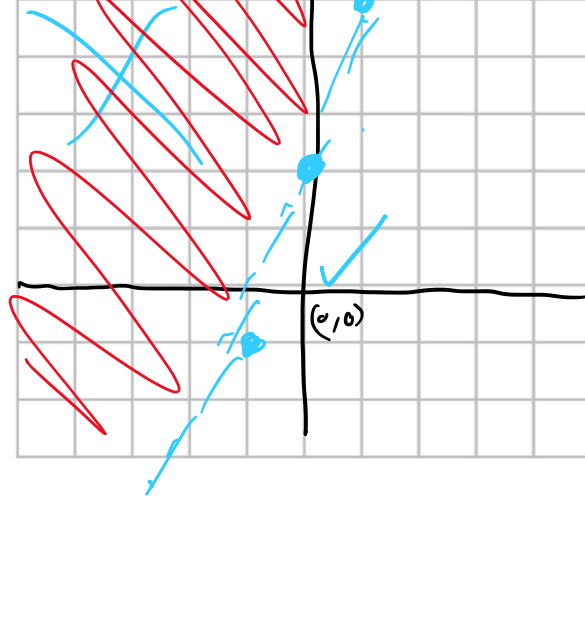
Points:  $(-3, 4)$ ,  $(0, 2)$ ,  $(-5, 3)$

$$y < 3x + 2$$

draw line  
→ solid / dashed  
2, ≤, >, <

$$(0, 0)$$

$$0 < 0 + 2 \quad \checkmark$$



The line that separates valid solution points from invalid points is called the boundary line.

If the line itself is a solution, ( $\geq, \leq$ ) then the boundary line should be solid.

If the line itself is not a solution, ( $>, <$ ) then the boundary line should be dashed.

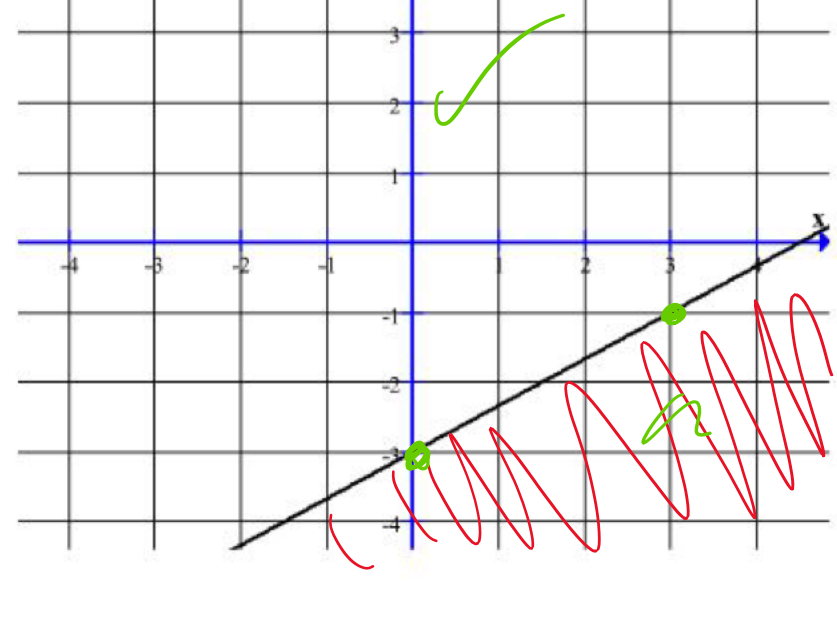
The algorithm:

EG:	$2x + 3y \leq 6$
Solve for y	$3y \leq 6 - 2x$ $y \leq -\frac{2}{3}x + 2$
Decide if you need a solid or dotted line	Solid $0 \leq 0 + 2$
Draw your line	
Decide which part of the graph contains valid solutions	
Scratch out the 'garbage'.	

EG:	$5x - 20y < 0$
Solve for y	$-20y < -5x$ $y > -\frac{5x}{20} = -\frac{1}{4}x$ $y > \frac{1}{4}x$
Decide if you need a solid or dotted line	dashed $(0, 1) > \frac{1}{4}$
Draw your line	
Decide which part of the graph contains valid solutions	
Scratch out the 'garbage'.	

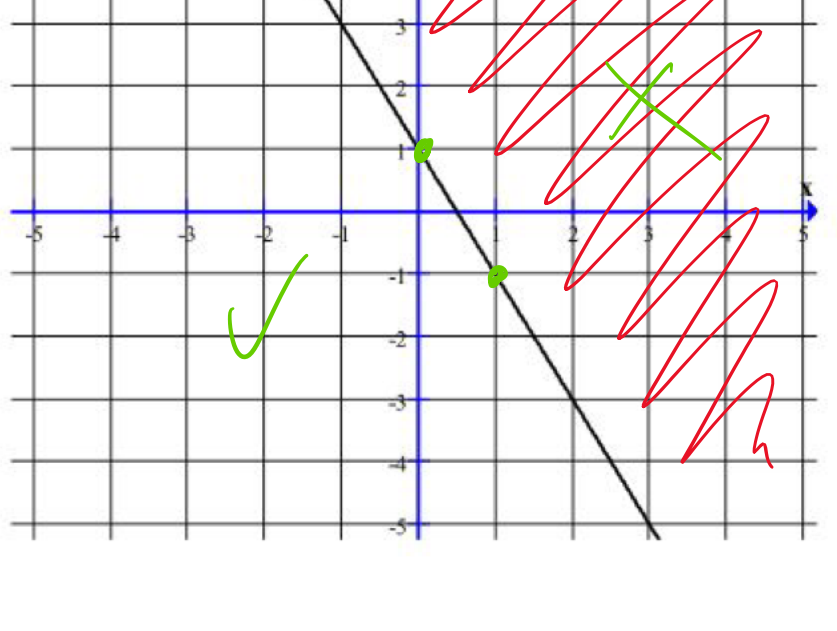
Write an inequality to represent the graph.

$$y \geq \frac{2}{3}x - 3$$



Write an inequality to represent the graph.

$$y \leq -2x + 1$$



HW Pg 472  
1, 6, 3, 4, 9, 11, 12