

Factoring - The End

For Now...

In our last section, I showed you a trick. I usually don't like to do that as when a student learns 'tricks' they use it all the time.

All of the questions I gave last class were selected to work. In general, it will not work.



The first question we did yesterday was $x^2 + 3x + 2$ and we saw that $m = 1$ and $n = 2$. Easy.

What if we simply added a 2 in front of x^2 ?

$$2x^2 + 3x - 2$$

You see how yesterday's trick won't work?

Let's try to reverse engineer what is going on...

$$\begin{aligned} & (2x - 1)(x + 2) \\ & = 2x^2 + \underline{4x} - x - 2 \\ & = 2x^2 + \underline{3x} - 2 \end{aligned}$$

The 3 comes from $2 \times 2 - 1 = 3$.

In general, a quadratic of the form $ax^2 + bx + c$ will require you to find 2 numbers, m and n , that multiply to $\underline{a \times c}$ and add to b .

This worked yesterday because I made sure that, for every question, $a = 1$. In general, that won't be true.

$$\begin{aligned} & \underline{2x^2} + \underline{3x} - 2 \\ & = \underline{2x^2 + 4x} - x - 2 \\ & = 2x(x+2) - (x+2) \\ & = (x+2)(2x-1) \end{aligned}$$

$n \cdot m = 2(-2) \checkmark$
 $n + m = 3 \checkmark$

$m = 4$
$n = -1$

→ Find 2 numbers, m and n, that multiply to $a \times c$ and add to b.

◆ $ax^2 + bx + c$

→ Since your numbers add to b. We can rewrite b as

$mx + nx$.

→ We know that we can factor by grouping as we chose m and n.

→ After group factoring, you better see that your 2 brackets have the same thing...

◆ ...or you done goofed.

→ Factor out the brackets that are the same.

◆ Celebrate.

Lets Try:

$9x^2 - 9x - 10$ <p style="text-align: right; color: blue;">$m = -15$ $n = 6$</p> $= \underline{9x^2 - 15x} + \underline{6x - 10}$ $= 3x(3x - 5) + 2(3x - 5)$ $= (3x - 5)(3x + 2) \quad \checkmark$	$3x^2 - 16x - 12$ <p style="text-align: right; color: blue;">$m = -18$ $n = 2$</p> $= \underline{3x^2 - 18x} + \underline{2x - 12}$ $= 3x(x - 6) + 2(x - 6)$ $= (x - 6)(3x + 2) \quad \checkmark$
$4x^2 + 5x - 6$ <p style="text-align: right; color: green;">$m = 8$ $n = -3$</p> $= \underline{4x^2 + 8x} - \underline{3x - 6}$ $= 4x(x + 2) - 3(x + 2)$ $= (x + 2)(4x - 3)$	$2x^2 + 11x + 12$

Some hard problems:

$(x + 1)^2 - 8(x + 1) + 16$	$8(x - 3)^2 - 64(x - 3) + 128$
$7a^2x - 6a^2 - 7x + 6$	$x^4 - x^2 - 12$
$x^{4n} - y^{4n}$	

