

1) Vertex Form $y = a(x-h)^2 + k$

Transformations:

- | | |
|--|--|
| if a is negative graph is flipped. | if a is positive graph is not flipped. |
| If a is Greater than 1. Or less than -1, the graph is stretched. | If a is a fraction between 1 and -1 the graph is squashed. |
| If h is positive graph shifts to the left. | If h is negative graph shifts to the right. |
| If k is positive graph shifts up. | If k is negative graph shifts down. |

$$y = -3(x+4)^2 - 8$$

- It is flipped.
- It is stretched by a factor of 3.
- It is shifted 4 to the left
- It is shifted 8 down

$$y = \frac{1}{2}(x-2)^2 - 4$$

- 1) Find the vertex: $(2, -4)$
- 2) Find the axis of symmetry: $x = 2$
- 3) Find the domain: $\{x | x \in \mathbb{R}\}$
- 4) Find the range: $\{y | y \geq -4, y \in \mathbb{R}\}$
- 5) Find the min/max: $y = -4$
- 6) Graph it.

	x	y
+1	4	-2
+1	3	-3.5
	2	-4
-1	1	-3.5
-1	0	-2

$$y = \frac{1}{2}((1)-2)^2 - 4$$

$$= \frac{1}{2}(1) - 4$$

$$= \frac{1}{2} - 4 = -3.5$$

$$y = \frac{1}{2}((0)-2)^2 - 4$$

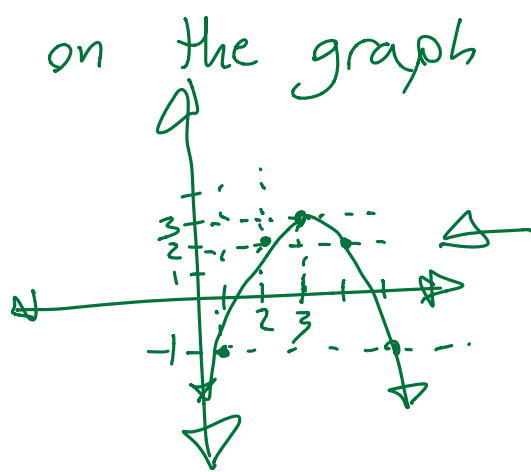
$$= 2 - 4$$

$$= -2$$

Use a vertex and a point on the graph to find a quadratic.

step 1: find the vertex

(3, 3)



$$y = a(x-h)^2 + k$$

$$y = a(x-3)^2 + 3$$

$$y = -1(x-3)^2 + 3$$

$$2 = a(2-3)^2 + 3$$

$$2 = a(-1)^2 + 3$$

$$2 = a(1) + 3$$

$$2 - 3 = a$$

$$a = -1$$

standard form = $y = ax^2 + bx + c$

$$y = x^2 + 8x - 7$$

complete the \square

$$y = (x^2 + 8x) - 7$$

$$y = (x^2 + 8x + 16) - 16 - 7$$
$$= (x+4)^2 - 23$$

$$\left(\frac{b}{2}\right)^2 = \left(\frac{8}{2}\right)^2 = 16$$

$$\pm\sqrt{16} = \pm 4$$

$$\downarrow$$
$$+4$$

$$y = 2x^2 + 16x - 7$$
$$= (2x^2 + 16x) - 7$$

$$\left(\frac{b}{2}\right)^2 = \left(\frac{8}{2}\right)^2 = 16$$

$$= 2(x^2 + 8x) - 7$$

$$= 2(x^2 + 8x + 16 - 16) - 7$$

$$= 2\left[\underbrace{(x^2 + 8x + 16)}_{(x+4)^2} - 16\right] - 7$$

$$= 2(x+4)^2 - 16(2) - 7$$

$$= 2(x+4)^2 - 39$$

Word problem

- throw ball
- lens / arc
- Revenue

Pg 157 #4

Pg 174 #5

Pg 193 # 3, 4, 6