

A nickel of mass 1.0 g is placed on a record of radius 12 cm, if the record rotates at 30 rpm (revolutions per minute) what minimum coefficient of friction is necessary to prevent the coin from sliding off?

$$m = 1.0 \text{ g} \quad r = 12 \text{ cm} \quad 30 = \text{rpm} \quad \mu = ?$$

$$30 \text{ rpm} = \frac{30 \text{ cycles}}{60 \text{ seconds}} = .5 \text{ Hz} \rightarrow f$$

$$\mu g = 4\pi^2 r f^2$$

$$\mu = \frac{4\pi^2 (12 \times 10^{-2}) (.5)^2}{9.8} = .12$$

A lamborghini of mass 1000 kg travels through a corner of radius 50 m, at what maximum speed can it travel if the coefficient of friction is 0.85 between the tires and road?

$$m = 1000 \text{ kg} \quad r = 50 \text{ m} \quad \mu = .85 \quad v = ?$$

$$F_c = F_f$$

$$\frac{v^2}{r} = \mu g$$

$$v = \sqrt{\mu g r}$$

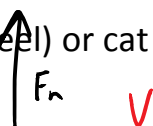
$$= \sqrt{.85 (9.8) (50)}$$

$$= 20.4 \text{ m/s}$$

## Vertical Circles:

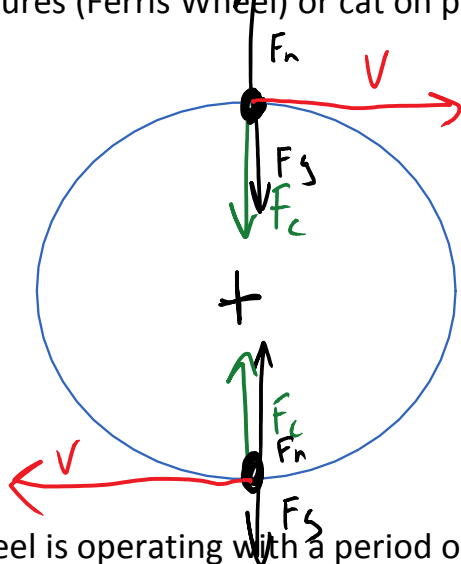
Draw the free body diagram, if you don't, you are choosing to get it wrong.

Rigid Structures (Ferris Wheel) or cat on pole:



$$\text{Top } F_c = F_g - F_n \quad \text{away from}$$

Rigid Structures (Ferris Wheel) or cat on pole:



Top  $F_c = F_g - F_n$  ↑ away from center

$F_{net} = W - L$  ↓ toward center

Bottom  $F_c = F_n - F_g$

A ferris wheel is operating with a period of 60 seconds and radius 15 m, calculate the normal force on a 70 kg mass at the top and bottom of the path.

$T = 60$     $r = 15\text{m}$     $F_n = ?$     $m = 70$   
↳ top/bottom

$F_{c_{top}} = F_g - F_n$

$\frac{70(4)\pi^2 r}{T^2}$

$ma_c = m a - F_n$

$70(4\pi^2 r f^2) = 70(9.8) - F_n$

$F_n = 674\text{N}$

$F_{c_{bot}} = F_n - F_g$

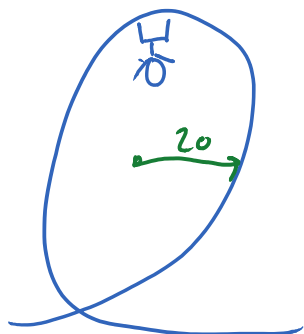
$70(4\pi^2 r f^2) = F_{n_{bot}} - 70(9.8)$

$F_{n_{bot}} = 698\text{N}$

What minimum speed must riders have so that

What minimum speed must riders have so that upside down riders don't fall out?

The upside down ride: top point only



$$F_c = F_g - F_n \rightarrow \underline{F_n = 0}$$

~~$$ma_c = mg$$~~

$$\frac{v^2}{r} = g$$

$$v = 14 \text{ m/s}$$

$$\frac{v^2}{20} = 9.8$$

~~Mass~~ = Kyle 66 kg = mass

Vomit comet  
OK go.

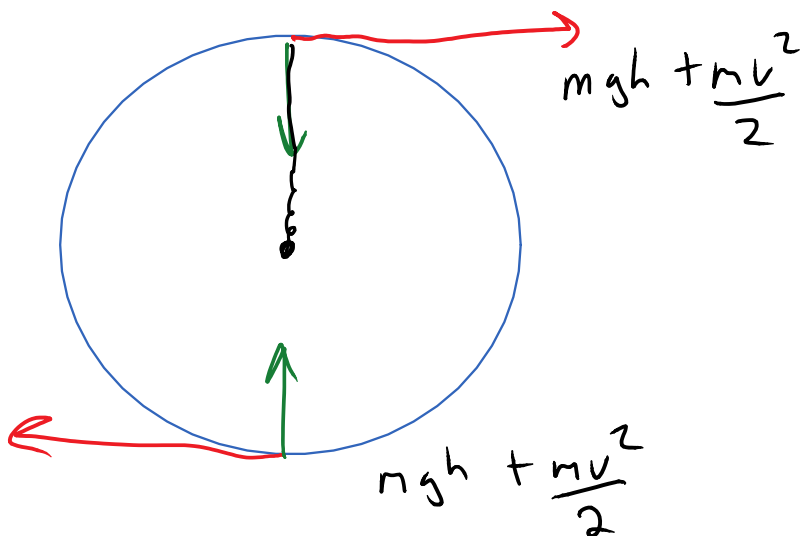
Weight =  $F_g$

Weightless =  $F_n = 0$

Objects (cats) swung on a rope:

The velocity of an object in vertical circle on a rope is usually NOT constant. It changes from the top to the bottom using the **Law of Conservation of Energy**.





The slowest you can be at the top;  $F_T = 0$

Top: there is a minimum speed  
At the top of the circle and at that  
Speed  $F_T = 0$  N

What minimum speed must you swing a 5 kg cat on a 60 m leash to go through the circle?

$$F_c = F_g + F_T \quad \left\{ \begin{array}{l} \text{set equal to} \\ \text{zero.} \end{array} \right. \quad \left| \quad \begin{array}{l} \cancel{m} a_c = \cancel{m} g \\ \frac{v^2}{r} = g \rightarrow v = 3.13 \frac{m}{s} \end{array} \right.$$

What is the  $F_T$  when the cat reaches the bottom?

1) Use conservation of energy to find  $v$  @ bottom.

$$\cancel{5}(9.8)(2) + \frac{\cancel{5}(3.13)^2}{2} = 0 + \frac{\cancel{5} v_f^2}{2}$$

$$v_f = 7.0 \text{ m/s}$$

2)  $F = W - L$

$$F_c = F_T - F_g$$

$$m a_c = F_T - m g$$

$$5 \left( \frac{7.0^2}{60} \right) = F_T - 5(9.8)$$

$$F_T = 294 \text{ N}$$